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Dissociation Equilibrium and the Activities of Sodium Fluoride and Aluminum(III) Fluoride in Molten Cryolite

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A method for calculating the stabilities of complex ions in binary molten salt mixtures, based on accurate enthalpy of mixing data, has been developed. As an example two different dissociation models for molten cryolite, (I) Na₃AlF₆(I) = $3NaF(1) + AlF_3(1)$ and (II) $Na_3AlF_6(1) = 2NaF(1) + NaAlF_4(1)$, have been tested. Good agreement between experimental and calculated data is obtained for model I by use of an enthalpy of dissociation, $\Delta H^{diss} = 22,000$ cal, and a degree of dissociation, $\alpha = 0.31$. This model is also in accordance with calorimetrically measured enthalpies of mixing for the process $\frac{1}{3}$ NaAlF₆(l) + $\frac{2}{3}$ AlF₃(l) = NaAlF₄(l).

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Introduction

The fairly large negative enthalpies of mixing, which were observed in the system NaF-Na₃AlF₆ by the present author,¹ could at first seem surprising because one would expect rather small enthalpies of mixing in anion mixtures with a common cation.

Kleppa and Melnichack² have shown that the enthalpies of mixing in such systems usually are of the order of 0-100 cal. In the following the observed ΔH^{M} will therefore be related to the dissociation of Na₃AlF₆ in the molten state.

Grjotheim³ made an approach to this problem 15 years ago. He discussed the most probable dissociation schemes for cryolite and also gave equations for the different dissociation models. Of the four models

 $2AlF_6^{3-} = Al_2F_{11}^{5-} + F^{-}$ $AlF_6^{3-} = AlF_5^{2-} + F^ AlF_6^{3-} = AlF_4^{-} + 2F^{-}$

 $A1F_6^{3-} = A1^{3+} + 6F^{-}$

he concluded that the dissociation scheme $AlF_6^{3-} = AlF_4^{-} +$ $2F^-$ would be the most probable model for molten cryolite.

Different approaches to this problem by Foster and Frank⁴ (density), Frank and Foster⁵ (electrical conductivity), and Rolin[°] (thermodynamic calculations) have given further evidence for the credibility of this dissociation scheme. However, it should be pointed out that all approaches to the problem of dissociation of the cryolite anion until now have been based on assumptions, like ideality of the molten mixture.

Method of Calculation

In Figure 1 is shown enthalpy of mixing curves for a system consisting of two molten salts AX and BX_m with an intermediate compound $A_n BX_{m+n}$. Curve I corresponds to the curve one would obtain if the compound $A_n B X_{m+n}$ was formed without dissociation of the complex $(BX_{m+n})^{n-1}$. In this case the enthalpy of mixing is equal to the enthalpy of formation of the complex

 $nAX(1) + BX_m(1) = A_n BX_{m+n}(1)$ with

(1) J. L. Holm, Ph.D. Thesis, Institute of Inorganic Chemistry, The Technical University of Norway, Nov 1971.
(2) O. J. Kleppa and M. Melnichack, J. Chem. Phys., 57, 5321

- (1972).
- (3) K. Grjotheim, Kgl. Nor. Vidensk. Selsk. Skr., No. 5, (1956).
- (4) P. A. Foster, Jr., and W. B. Frank, J. Electrochem. Soc., 107, 997 (1969).

(5) W. B. Frank and L. M. Foster, J. Phys. Chem., 64, 310 (1960).

(6) M. Rolin, Bull. Soc. Chim. Fr., 681 (1960).

$$\Delta H_{\rm r} = \Delta H^{\rm M} \tag{1}$$

If, however, the complex is not a very strong one, one would obtain a curve like the one shown as curve II. Enthalpy of mixing curves of this type were for instance found by Kleppa and McCarty⁷ in the three systems KCl-MgCl₂, RbCl-MgCl₂, and CsCl-MgCl₂. The complex $A_n BX_{m+n}$ may, for instance, dissociate in the molten state as given by equilibrium I or equilibrium II

$$BX_{m+n}^{n-} = BX_{m+1}^{-} + (n-1)X^{-}$$

$$1 - \alpha_{0} \qquad \alpha_{0} \qquad (n-1)\alpha_{0}$$
(I)

$$\begin{aligned} \mathbf{D}\mathbf{x}_{m+n} &= \mathbf{D}\mathbf{x}_m + n\mathbf{X} \\ 1 - \alpha_0 & \alpha_0 & n\alpha_0 \end{aligned} \tag{II}$$

where α_0 is the degree of dissociation. The corresponding equilibrium constants K_{I} and K_{II} are

$$K_{\rm I} = C_{\rm I} \cdot \frac{\alpha_0}{1 - \alpha_0} \left[\frac{(n-1)\alpha_0}{1 + (n-1)\alpha_0} \right]^{n-1}$$
(2)

$$K_{\rm II} = C_{\rm II} \cdot \frac{\alpha_0}{1 - \alpha_0} \left[\frac{n\alpha_0}{1 + n\alpha_0} \right]^n \tag{3}$$

Here the factors C_{I} and C_{II} contain the product of the activity coefficients.

In a mixture of the complex $A_n BX_{m+n}$ with either AX or BX_m the dissociation equilibrium I or II will be shifted to the left, and usually the complex will be less dissociated in the mixture. The degree of dissociation will change with composition. The enthalpy of mixing as a function of composition, ΔH^{M}_{C} , is then given by eq 4. Here ΔH^{diss}

$$\Delta H^{\rm M}{}_{\rm C} = \Delta H^{\rm diss} N_0(\alpha_0 - \alpha) \tag{4}$$

is the enthalpy of dissociation of the pure complex, N_0 is the weighed-in mole fraction of the complex, and α_0 and α are the degrees of dissociation in the pure complex and in the mixture, respectively.

In Figure 1 the dashed curve represents the enthalpy of mixing one would have gotten in the hypothetical case when the degree of dissociation is independent of composition. Curve II represents the curve one obtains if α is smaller than α_0 . The difference between the dashed line and curve II therefore represents the enthalpy one will obtain if the pure complex is mixed with one of the components.

Dissociation Models for Molten Cryolite

In the following some of the dissociation models given above will be discussed and tested in connection with the

(7) O. J. Kleppa and F. G. McCarty, J. Phys. Chem., 70, 1249 (1966).



Figure 1. Enthalpy of mixing curves for a system $AX-BX_m$ with an intermediate compound $A_nBX_{(n+m)}$.

measured enthalpies of reactions in the system NaF-Na₃AlF₆. Here the discussion will be limited to the two most probable models¹ which are

$$Na_{3}AlF_{6}(l) \neq 3NaF(l) + AlF_{3}(l)$$
(I)

$$Na_{3}AlF_{6}(l) \neq 2NaF(l) + NaAlF_{4}(l)$$
(II)

In putting up these equations it should be pointed out that according to calculations by the present author^{1,8,9} NaAlF₄ should be unstable with respect to Na₃AlF₆ and AlF₃, since the enthalpy of the reaction

$$Na_3AlF_6(l) + 2AlF_3(l) = 3NaAlF_4(l)$$
 (III)

is of the order $12 \pm 4 \text{ kcal mol}^{-1}$ at 1273 K. This can very easily be seen from enthalpy cycle 1. The cycle gives eq 5. cycle 1

 $\Delta H_1 = \Delta H_f(\text{mixture}) - \Delta H_f(\text{Na}_3\text{AlF}_6) - 2\Delta H_f(\text{AlF}_3)$ (5) By inserting the experimental values $\Delta H_f(\text{mixture}) = 61.5$ kcal,⁹ $\Delta H_f(\text{Na}_3\text{AlF}_6) = 27.1$ kcal mol⁻¹,^{10,11} and $\Delta H_f(\text{AlF}_3) =$ 11.3 kcal mol⁻¹,⁹ one obtains for reaction III $\Delta H_1 = +12.0$ kcal.

For schemes I and II the dissociation constants are

$$K_{\rm I} = C_{\rm I} \cdot \frac{\alpha_0}{1 - \alpha_0} \cdot \left(\frac{3\alpha_0}{1 + 3\alpha_0}\right)^3 \tag{6}$$

$$K_{\rm II} = C_{\rm II} \cdot \frac{\alpha_0}{1 - \alpha_0} \cdot \left(\frac{2\alpha_0}{1 + 2\alpha_0} \right) \tag{7}$$

In a mixture of cryolite and sodium fluoride, where the mole fractions are $N_0(Na_3AlF_6)$ and $N_1(NaF)$, the degree of dissociation is α_1 .

For this mixture the dissociation constants for the two schemes are given by

$$K^{\circ}_{I} = \frac{\alpha_{1}}{1 - \alpha_{1}} \cdot \left(\frac{3N_{0}\alpha_{1} + N_{1}}{1 + 3\alpha_{1}N_{0}}\right)^{3}$$
(8)

(8) J. L. Holm, Acta Chem. Scand., in press.

(9) J. L. Holm, *High Temp. Sci.*, submitted for publication. (10) C. J. O'Brien and K. K. Kelley, J. Amer. Chem. Soc., 79,

(10) C. J. O Brien and K. K. Kelley, J. Amer. Chem. Soc., 79, 5616 (1957).

(11) B. J. Holm and F. Gronvold, Acta Chem. Scand., in press.

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$$K^{\circ}_{II} = \frac{1}{1 - \alpha_1} \cdot \left(\frac{2N_0 \alpha_1 + N_1}{1 + 2N_0 \alpha_1} \right)^2 \tag{9}$$

The theoretical enthalpy of mixing, ΔH^{M}_{C} , can be calculated from the following expression

$$\Delta H^{\rm M}{}_{\rm C} = -\Delta H^{\rm diss} N_0(\alpha_0 - \alpha_1) \tag{10}$$

where ΔH^{diss} is the enthalpy for the dissociation of Na₃AlF₆, according to scheme I or II.

In writing the expression for the equilibrium constants, eq 8 and 9, the mole fractions have been used instead of the activities. The correct equilibrium constants are given by eq 11 and 12.

$$K_{\rm I} = K^{\circ}_{\rm I} \cdot \frac{\gamma_{\rm NaF}^{3} \cdot \gamma_{\rm AIF_{3}}}{\gamma_{\rm Na_{3}AIF_{6}}}$$
(11)

$$K_{\rm II} = K^{\circ}_{\rm II} \cdot \frac{\gamma_{\rm NaF}^2 \cdot \gamma_{\rm NaAlF_4}}{\gamma_{\rm Na_3AlF_6}}$$
(12)

It has been assumed that the change with composition in the term containing the product of the activity coefficients is negligible. As shown in the Appendix, this is indeed the case. For model I the true equilibrium constant is given by

$$K_{\rm I}^{a} = K_{\rm I} \cdot 10^{-3.75 \pm 0.1} \tag{13}$$

For the calculation of $\Delta H^{M}{}_{C}$ a computer program was made. The calculations were performed in the following manner. A set of values was chosen for ΔH^{diss} . For each of these values of ΔH^{diss} the following operation was performed for each of a set of values of α_0 . The equation 6 =8 or 7 = 9 was solved with respect to α_1 for values of N_0 from 0 to 1. This value of α_1 was then used to calculate $\Delta H^{M}{}_{C}$ as a function of ΔH^{diss} , α_1 , N_0 , and α_0 . From the results could be found the combination of values for α_0 and ΔH^{diss} which gave the best fit between the experimental enthalpies of mixing and the calculated curve.

For scheme I, $AIF_6^{3-} = AIF_3 + 3F^-$, the best fit is found for $\alpha_0 = 0.31 \pm 0.01$ and $\Delta H^{diss} = 22,000 \pm 1000$ cal (Table I). As can be seen from Figure 2 the agreement between the calculated and experimental results is good. The value for ΔH^{diss} is in excellent agreement with that calculated from a thermodynamic cycle by the present author¹ (cycle 2). cycle 2

ΛH.

$$\Delta H_2^{M} = \Delta H_2 + 3\Delta H_f(\text{NaF}) + \Delta H_f(\text{AlF}_3) - \Delta H_f(\text{Na}_3 \text{AlF}_6)$$
(14)

By inserting $\Delta H_2 = 13.8 \text{ kcal mol}^{-1}, ^{12} \Delta H_f(\text{Na}_3\text{AlF}_6) = 27.1 \text{ kcal mol}^{-1}, ^{1.0,11} \Delta H_f(\text{NaF}) = 8.0 \text{ kcal mol}^{-1}, ^{10,11} \text{ and } \Delta H_f(\text{AlF}_3) = 11.3 \text{ kcal mol}^{-1}, ^{9} \text{ one obtains } \Delta H_2^M = 22.0 \text{ kcal.}$ For scheme II, $\text{AlF}_6^{3-} = \text{AlF}_4^- + 2\text{F}^-, \Delta H^{\text{diss}}$ has been set equal to 18,000 cal, which is the difference between the enthalpies calculated from cycle 1 and cycle 2. The best fit is obtained for $\alpha_0 = 0.35$. As can be seen from Figure 2, however, the ΔH^M_C values calculated for this scheme are less negative than the experimental enthalpies of mixing. Hence, this model does not explain the rather large negative enthalpies of mixing which are observed in the system.

(12) JANAF Thermochemical Tables, Clearinghouse, Springfield, Va., 1972.

Na₃AlF₆

Table I. Dissociation Degrees and Calculated Enthalpies of Mixing, in cal mol⁻¹, on the NaF Side



NaF

Figure 2. Experimental and calculated ΔH^{M} curves for molten mixtures of Na₃AlF₆ and NaF: \bigcirc , experimental values; heavy line, least-squares ΔH^{M} curve; thin line, best calculated ΔH^{M} curve for dissociation scheme AlF₆³⁻ = AlF₃ + 3F⁻, $\alpha_0 = 0.31$ and $\Delta H^{diss} =$ 22,000 cal; dotted line, best calculated ΔH^{M} curve for dissociation scheme AlF₆³⁻ = AlF₄⁻ + 2F⁻, $\alpha_0 = 0.35$ and $\Delta H^{diss} = 18000$ cal.

The calculated mole fractions of NaF, Na₃AlF₆, and AlF₃ in NaF-Na₃AlF₆ melts at 1011°, for $\alpha_0 = 0.31$ and $\Delta H^{diss} =$ 22,000 cal (scheme I), are plotted in Figure 3 as a function of composition. Hence, of the two most probable dissociation schemes for molten cryolite

$$Na_3AlF_6(1) = 3NaF(1) + AlF_3(1)$$
 (1)

$$Na_3AIF_6(1) = 2NaF(1) + NaAIF_4(1)$$
 (II)

scheme II seems to be of minor importance on the NaF side of the system. The main species present in basic (NaF rich) melts will be Na^+ , AlF_6^{3-} , F^- , and " AlF_3 ." (In this dissociation scheme "AlF₃" is not supposed to be a separate species, but rather the inner and most stable part of the distorted AlF_6^{3-} complex.)

The dissociation equilibrium $AlF_6^{3-} = AlF_3 + 3F^-$ with a calculated dissociation constant of 10^{-5} at 1011° (see Appendix) is written *thermodynamically*. This preferred dissociation indicates that the Al-F vibrations in the AlF_6^{3-} complex follow a model of type I

 $(AlF_{5}^{3^{-}}) \rightleftharpoons [(AlF_{3})(F^{-})_{3}]$ octahedral distorted octahedral

rather than type II.

 $(AlF_6^{3-}) \rightleftharpoons [(AlF_4)^{-} + 2F^{-}]$ octahedral tetrahedral

Spectroscopically one would therefore expect to observe AlF_6^{3-} in a distorted octahedral field as illustrated above. The more or less free AlF_3 which is formed could be compared to BF_3 , a planar molecule with an incomplete octet around the boron atom. As there is not a full octet, there will be fewer repulsions between the electrons, and the length of the Al-F bond will be somewhat shortened. Con-

Figure 3. Mole fractions of NaF, Na₃AlF₆, and AlF₃ in molten mixtures of NaF and Na₃AlF₆ according to scheme I, $AlF_6^{3-} = AlF_3 + 3F^-$, $\alpha_0 = 0.31$, $\Delta H^{diss} = 22000$ cal.

Weighed in mol fraction Na_3AlF_6 (N₀)



Figure 4. Dissociation model for molten cryolite, $AlF_6^{3-} = "AlF_3" + 3F^-$.

sequently, in the deformed or distorted AlF_6^{3-} complex there should be three shorter and three longer Al-F bonds, as illustrated in Figure 4.

Registry No. NaF, 7681-49-4; AlF₃, 7784-18-1; Na₃AlF₆, 13775-53-6; cryolite, 15096-52-3.

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Appendix

a. Activity Coefficients γ_{NaF} , γ_{AIF_3} , and $\gamma_{Na_3AIF_6}$ in Liquid Ternary NaF-AIF₃-Na₃AIF₆ Mixtures. The partial excess Gibbs free energy for component A in a ternary mixture A-B-C can be calculated from the expression

$$\overline{G}^{E}{}_{A} = R'T \log \gamma_{A} = (1 - X_{A})(X_{B}\lambda_{AB} + X_{C}\lambda_{AC}) - X_{B}X_{C}\lambda_{BC}$$
(15)

Table II. Activity Coefficients of NaF, AlF_3 , and Na_3AlF_6 in Molten Mixtures of Sodium Fluoride and Cryolite

Weighed- in mol fraction of Na ₃ AlF ₆ , N_0	Log YNaF	Log ƳAlF3	Log γNa3AlF6	$\frac{\gamma_{\text{NaF}}^3 \cdot \gamma_{\text{A1F}_3}}{\gamma_{\text{Na}_3 \text{A1F}_6}}$
0.2	(-0.01)ª	(-4.0) ^a	(+0.07) ^a	(10 ^{-4.1})
0.4	-0.090	-3.18	+0.167	$10^{-3.7}$
0.6	-0.215	-2.72	+0.284	$10^{-3.7}$
0.3	-0.337	-2.35	+0.351	10-3.8
1.0	-0.436	-2.12	+0.407	10-3.8

^a Uncertain value.

(see, for instance, ref 13 and 14). Here X_A , X_B , and X_C are the ternary mole fractions of the components in the system, while the λ 's are the interaction parameters in the component binaries. Equation 15 has been used to calculate the activity coefficients γ_{NaF} , γ_{AlF_3} , and $\gamma_{Na_3AlF_6}$ in the ternary mixture at different compositions.

The binary interaction parameters λ_{AC} and λ_{BC} [A = NaF, B = AlF₃, C = Na₃AlF₆ (undissociated)] have been assumed to be small compared to λ_{AB} (*i.e.*, $\lambda_{AC} = \lambda_{BC} = 0$). The interaction parameter in the NaF-rich part of the system NaF-AlF₃ has been calculated from enthalpy data obtained by the present author⁹ and follows the expression

$$\lambda_{\text{NaF-AIF}_3} = -28,410 - 42,130X_{\text{AIF}_3} + 176,280X_{\text{AIF}_3}^2 \text{ cal}$$
(16)

The mole fractions used in the calculations have been taken from Figure 3. The calculated activity coefficients are given in Table II. Using these values, one can now calculate the activities of sodium fluoride and aluminum fluoride in pure molten cryolite.

$$a_{\text{NaF}} = N_{\text{NaF}} \cdot \gamma_{\text{NaF}} = 0.48 \times 10^{-0.436} = 0.176$$
(17)

$$a_{A1F_3} = N_{A1F_3} \cdot \gamma_{A1F_3} = 0.16 \times 10^{-2.12} = 1.2 \times 10^{-3}$$
 (18)

The activity coefficients can be checked by calculating the activity of Na_3AlF_6 in a pure cryolite melt, which should be 1.0. From the data given in this paper one obtains

$$a_{\text{Na},\text{AlF}_{4}} = 0.36 \times 10^{0.407} = 0.92 \tag{19}$$

This shows that the activity coefficients given are somewhat uncertain. These uncertainties in the activities are mainly due to the interaction parameter which has been used (eq 15). This interaction parameter is based on enthalpy data and not, as it more correctly ought to be, on Gibbs free energy data. Even so, these data are probably the best activity values for the cryolite melt reported until now, as the errors are certainly less than 10%.

(13) J. Guion, M. Blander, D. Hengstenberg, and K. Hagemark, J. Phys. Chem., 72, 2086 (1968).

(14) K. Hagemark, J. Phys. Chem., 72, 2316 (1968).

Kvande¹⁵ has reported a vapor pressure of AlF₃ above a cryolite melt, $p_{A1F_3} = 0.012$ Torr, while the total pressure of AlF₃ above solid AlF₃ at the same temperature, according to Kuxmann and Tillessen,¹⁶ is p = 10.5 Torr. This gives an activity of AlF₃ in molten cryolite of the order of 10^{-3} , in good accordance with the value 1.2×10^{-3} given above.

One may therefore with good accuracy use an equilibrium constant of

$$K_{\rm eq} = \frac{a^{3} {}_{\rm NaF} \cdot a_{\rm AIF_{3}}}{a_{\rm Na_{3}} {}_{\rm AIF_{6}}} = [(0.176)^{3}] 1.2 \times 10^{-3} \simeq 10^{-5}$$
(20)

for the dissociation equilibrium of molten cryolite Na₃-AlF₆(1) \neq 3NaF(1) + AlF₃(1).

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b. An Equation for Calculating Liquidus Curves on the Cryolite Side of Phase Diagrams. In calculations of phase diagrams where cryolite is the main component, it is necessary to have a correct expression for the mole fraction of cryolite in the mixture. This mole fraction can be expressed as

$$\dot{N}_{Na_{3}AlF_{6}} = k \cdot N_{Na^{+}}^{3} \cdot N_{AlF_{6}}^{3-}$$
(21)

In pure molten cryolite $N_{\text{Na}_3\text{AlF}_6} = 1$, $N_{\text{Na}^+} = 1$, and $N_{\text{AlF}_6} = (1 - \alpha_0)/(1 + 3\alpha_0)$. By use of the dissociation degree for the scheme AlF₆³⁻ = AlF₃ + 3F⁻, $\alpha_0 = 0.31$ at 1011°, one finds k = 2.80 and therefore

$$N_{\text{Na}_{3}\text{AlF}_{6}} = 2.80N_{\text{Na}^{+}}{}^{3} \cdot N_{\text{AlF}_{6}}{}^{3-}$$
(22)

The partial Gibbs free energy of cryolite is given by the wellknown expression

$$\overline{G}_{\operatorname{Na_3AlF_6}} = -\Delta H_{\mathrm{f}}(1 - T/T_{\mathrm{f}}) = \overline{H}_{\operatorname{Na_3AlF_6}} - T\overline{S}_{\operatorname{Na_3AlF_6}}$$
(23)

The liquidus curve in systems without solid solution can be calculated from

$$T = \frac{\Delta H_{\rm f} + \bar{H}_{\rm Na_3AIF_6}}{\Delta S_{\rm f} + \bar{S}_{\rm Na_3AIF_6}}$$
(24)

Here $\overline{H}_{Na_3AlF_6}$ is the partial enthalpy of mixing and ΔS_f is the entropy of fusion of cryolite. In this expression the partial entropy of mixing, $\overline{S}_{Na_3AlF_6}$, has also been introduced. In calculations the partial molar entropy, \overline{S} , is usually set equal to the configurational entropy, which in this case is

$$S_{\text{Na}_3\text{AlF}_6} = -R \ln N_{\text{Na}_3\text{AlF}_6} \tag{25}$$

By combining eq 22, 24, and 25 one obtains the following expression

$$T = \frac{\Delta H_{\rm f} + \overline{H}_{\rm Na_3A1F_6}}{\Delta S_{\rm f} - R \ln \left(2.80 \cdot N_{\rm Na^+}^3 \cdot N_{\rm AlF_6}^3\right)}$$
(26)

(15) H. Kvande, Lic. Thesis, Institute of Inorganic Chemistry, University of Trondheim, 1972.

(16) U. Kuxmann and U. Tillessen, Erzmetall, 20, 147 (1967).